wers the question. N

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers
Solve the problem. 1) How many players are there in the weighted voting system [34:10,7,4,4,3,3,3,1,1]? A) 36 B) 9 C) 10 D) 38 E) none of these Answer: B
Allswei. D
 2) How many players are there in the weighted voting system [20:7,5,4,4,2,2,2,1,1]? A) 10 B) 28 C) 9 D) 20 E) none of these
Answer: C
3) What is the quota in the weighted voting system [34:10,7,4,4,3,3,3,1,1]? A) 36 B) 34 C) 9 D) 10 E) none of these Answer: B
Allswer: b
 4) What is the quota in the weighted voting system [20:7, 5, 4, 4, 2, 2, 2, 1, 1]? A) 10 B) 20 C) 9 D) 28 E) none of these Answer: B
 5) The total number of votes in the weighted voting system [34:10,7,4,4,3,3,3,1,1] is A) 34. B) 10. C) 9. D) 36. E) none of these Answer: D
6) The total number of votes in the weighted voting system [20:7,5,4,4,2,2,2,1,1] is A) 20. B) 48.

C) 28. D) 10.

Answer: C

E) none of these

 7) In the weighted voting system [q: 10, 8, 6], a strict majority of the votes is needed to pass a motion. The value of the quota q is A) 11. B) 13. C) 10. D) 12. E) none of these Answer: B
8) In the weighted voting system [q:10, 8, 4], a strict majority of the votes is needed to pass a motion. The value of the quota q is A) 12. B) 13. C) 11. D) 10. E) none of these Answer: A
 9) In the weighted voting system [q: 20, 19, 16, 2, 1, 1], a two-thirds majority of the votes is needed to pass a motion. The value of the quota q is A) 40. B) 7. C) 59. D) 20. E) none of these Answer: A
 10) In the weighted voting system [q: 10, 9, 8, 1, 1], a two-thirds majority of the votes is needed to pass a motion. The value of the quota q is A) 7. B) 29. C) 20. D) 19. E) none of these Answer: C
 11) In the weighted voting system [q: 12, 10, 5, 1, 1], the smallest possible value that the quota q can take is A) 29. B) 15. C) 12. D) 14. E) none of these Answer: B
 12) In the weighted voting system [q: 12, 10, 5, 1, 1], the largest possible value that the quota q can take is A) 29. B) 30. C) 22. D) 15. E) none of these Answer: A

13) In the weighted voting system [q:10, 8, 5], the smallest possible value that the quota q can take is A) 12. B) 11. C) 13. D) 23. E) none of these
Answer: A
 14) In the weighted voting system [q: 24, 12, 8, 4, 2], the smallest possible value that the quota q can take is A) 25. B) 36. C) 24. D) 50. E) none of these Answer: E
15) In the weighted voting system [q : 22, 12, 8, 4], the smallest possible value that the quota q can take is A) 46. B) 31. C) 23. D) 22. E) none of these Answer: E
16) In the weighted voting system [q: 24, 12, 8, 4, 2], the largest value that the quota q can take is A) 25. B) 24. C) 50. D) 36. E) none of these Answer: C
17) In the weighted voting system [30 : 24, 12, 8, 4, 2], the minimum percentage of votes needed to pass a motion is A) 61%. B) 60%. C) 50%. D) 30%. E) 51%. Answer: B
18) In the weighted voting system [9:11, 4, 2],A) P₁ is a dictator.B) P₁ has veto power but is not a dictator.C) there are no dictators.
D) every player is a dictator. E) none of these Answer: A

- 19) In the weighted voting system [12:13, 7, 2],
 - A) every player is a dictator.
 - B) P₁ has veto power but is not a dictator.
 - C) there are no dictators
 - D) P₁ is a dictator.
 - E) none of these

Answer: D

- 20) In the weighted voting system [12:11, 5, 5],
 - A) every player has veto power.
 - B) P₁ is a dictator.
 - C) no player has veto power.
 - D) P₁ has veto power but is not a dictator.
 - E) none of these

Answer: D

- 21) In the weighted voting system [13:12, 7, 2],
 - A) P₁ has veto power but is not a dictator.
 - B) P₁ is a dictator.
 - C) no player has veto power.
 - D) every player has veto power.
 - E) none of these

Answer: A

- 22) In the weighted voting system [14:7,7,6],
 - A) P₁ and P₂ have equal power, P₃ is a dummy.
 - B) P₁ and P₂ have equal power, P₃ is not a dummy.
 - C) P₁ has all the power, P₂ and P₃ are dummies.
 - D) all three players have equal power.
 - E) none of these

Answer: A

- 23) In the weighted voting system [100 : 50, 50, 48],
 - A) all three players have equal power.
 - B) P₁ and P₂ have equal power, P₃ is not a dummy.
 - C) P₁ and P₂ have equal power, P₃ is a dummy.
 - D) P₁ has all the power, P₂ and P₃ are dummies.
 - E) none of these

Answer: C

- 24) In the weighted voting system [10:5,4,2],
 - A) P₁ has veto power, P₃ is a dummy.
 - B) P₁ and P₂ have veto power, P₃ is a dummy.
 - C) all three players have veto power.
 - D) no player has veto power.
 - E) none of these

25) In the weighted voting system [11 : 5, 4, 2], A) P_1 and P_2 have veto power, P_3 is a dummy.	
B) only P ₁ has veto power.	
C) no player has veto power.D) all three players have veto power.E) none of these	
Answer: D	
26) In the weighted voting system [q: 24, 12, 8, 4, 2], what is the smallest possible value of the quota q for whi	ich P5
is a dummy? A) 27 B) 30 C) 29 D) 24 E) none of these	
Answer: A	
 27) In the weighted voting system [q: 24, 12, 8, 4, 2], what is the smallest possible value of the quota q for whi and P₅ are dummies? A) 29 B) 27 C) 24 D) 31 	.ch P4
E) none of these	
Answer: D	
28) In the weighted voting system [q : 24, 12, 6, 3], what is the largest possible value of the quota q for which I dummy? A) 40 B) 42 C) 39 D) 41 E) none of these	' ₄ is a
Answer: B	
29) What is the smallest value of w for which P ₄ is not a dummy in the weighted voting system [30 : 24, 12, 6, A) 3 B) 6 C) 5 D) 1 E) none of these	w]?
Answer: B	

30) In the weighted voting system [q:7,5,3,2,1], every player has veto power. The value of the quota q is A) 17. B) 15. C) 10. D) 18. E) none of these Answer: D
31) In the weighted voting system [q: 6, 5, 4, 3, 2, 1], every player has veto power. The value of the quota q is A) 11. B) 21. C) 20. D) 22. E) none of these Answer: B
32) In the weighted voting system [q:7,5,3,2,1], no player has veto power. The largest possible value that the quota q can take is A) 17. B) 9. C) 11. D) 10. E) none of these Answer: C
33) In the weighted voting system [q: 6, 5, 4, 3, 2, 1], no player has veto power. The largest possible value that the quota q can take is A) 15. B) 11. C) 13. D) 17. E) none of these Answer: A
34) A board is made up of two women (W) and three men (M). In order to pass a motion, three of the five including at least one woman must vote "yes". Which of the following weighted voting systems represent this situation? A) [6:3,3,2,2,2] B) [3:1,1,1,1,1] C) [7:3,3,2,2,2] D) [8:3,3,2,2,2] E) none of these Answer: C

A committee consists of six members (A, B, C, D, E, and F). A has veto power; B, C, D, and E each have one vote. F is a nonvoting member. For a motion to pass it must have the support of A plus at least two additional voting members.

- 35) A weighted system that could represent this situation is
 - A) [5:3, 1, 1, 1, 1, 0].
 - B) [6:3, 1, 1, 1, 1, 0].
 - C) [6:5, 1, 1, 1, 1, 0].
 - D) [4:2, 1, 1, 1, 1, 0].
 - E) none of these

Answer: A

Solve the problem.

- 36) A player whose weight is bigger than the weight of every other player
 - A) is a dictator.
 - B) is a critical player in every winning coalition.
 - C) has veto power.
 - D) is a dummy.
 - E) none of these

Answer: E

- 37) Consider the generic weighted voting system $[q:w_1,w_2,\ldots,w_N]$. Which of the following mathematical statements is equivalent to saying that P_1 is a dictator?
 - A) $w_1 \ge q$
 - B) $w_2 + w_3 + ... + w_N < q$ and $w_1 < q$
 - C) $w_1 > w_2$
 - D) $w_1 > q$
 - E) none of these

Answer: A

- 38) Consider the generic weighted voting system $[q:w_1,w_2,\ldots,w_N]$. Which of the following mathematical statements is equivalent to saying that P_1 has veto power?
 - A) $w_2 + w_3 + ... + w_N < q$ and $w_1 < q$
 - B) $w_1 > q$
 - C) $w_1 \ge q$
 - D) $w_1 > w_2$
 - E) none of these

Answer: A

Refer to the weighted voting system [35:32,15,10,3] and the Banzhaf definition of power. (The four players are P_1 , P_2 , P_3 , and P_4 .)

- 39) The weight of the coalition $\{P_2, P_3, P_4\}$ is
 - A) 28.
 - B) 57.
 - C) 25.
 - D) 60.
 - E) none of these

- 40) The winning coalitions are:
 - A) all coalitions with two or more players.
 - B) all coalitions with two or more players, one of which is P₁.
 - C) all coalitions with three or more players.
 - D) all coalitions.
 - E) none of these

Answer: B

- 41) The number of winning coalitions is
 - A) 24.
 - B) 7.
 - C) 8.
 - D) 15.
 - E) none of these

Answer: B

- 42) Which players in the coalition {P₁, P₃} are critical?
 - A) P₃ only
 - B) P₁ only
 - C) P₁ and P₃
 - D) None of the players
 - E) none of these

Answer: C

- 43) Which players in the coalition {P₁, P₃, P₄} are critical?
 - A) P₁ only
 - B) None of the players
 - C) P₁ and P₃ only
 - D) All three players
 - E) none of these

Answer: A

- 44) The Banzhaf power distribution of the weighted voting system is
 - A) $P_1: 75\%; P_2: 8\frac{1}{3}\%; P_3: 8\frac{1}{3}\%; P_4: 8\frac{1}{3}\%.$
 - B) P₁: 70%; P₂: 10%; P₃: 10%; P₄: 10%.
 - C) P₁: 60%; P₂: 20%; P₃: 10%; P₄: 10%.
 - D) P₁: 40%; P₂: 20%; P₃: 20%; P₄: 20%.
 - E) none of these

Refer to the weighted voting system	[25 : 22, 12, 6, 3] and the Banzhaf	definition of power. (The fo	our players are P ₁ , P ₂ , P ₃ ,
and P4.)			

45) The weight of the coalition $\{P_2, P_3, P_4\}$ is	
A) 25.	
B) 40.	
C) 22.	
D) 21.	
E) none of these	
Answer: D	
46) The winning coalitions are	
A) all coalitions with three or more players.	
B) all coalitions with two or more players.	
C) all coalitions with two or more players, one of which is P	'1·
D) all coalitions.	
E) none of these	
Answer: C	
47) The number of winning coalitions is	
A) 8.	
B) 7.	
C) 15.	
D) 1.	
E) none of these	
Answer: B	
48) Which players in the coalition $\{P_1, P_2\}$ are critical?	
A) P ₁ only	
B) P ₁ and P ₂	
C) P ₂ only	
D) None of the players	
E) none of these	
Answer: B	
49) Which players in the coalition {P ₁ , P ₃ , P ₄ } are critical?	
A) All three players	
B) P ₁ only	
C) P ₁ and P ₃ only	
D) None of the players	
E) none of these	
Answer: B	

50) The Banzhaf power distribution of the weighted voting system is
A) P ₁ : 70%; P ₂ : 10%; P ₃ : 10%; P ₄ : 10%.
B) P ₁ : 60%; P ₂ : 20%; P ₃ : 10%; P ₄ : 10%.
C) P ₁ : 40%; P ₂ : 20%; P ₃ : 20%; P ₄ : 20%.
D) P ₁ : 25%; P ₂ : 25%; P ₃ : 25%; P ₄ : 25%.
E) none of these
Answer: A
Refer to the weighted voting system [14:5,5,4,4] and the Banzhaf definition of power. (The four players are P ₁ , P ₂ , P ₃
and P ₄ .)
51) What is the weight of the coalition {P ₂ , P ₃ , P ₄ }?
A) 13
B) 14
C) 8
D) 12
E) none of these
Answer: A
52) Which players in the coalition $\{P_1, P_2, P_3, P_4\}$ are critical?
A) P ₁ and P ₂
B) P ₁ only
C) None of the players
D) All four players
E) none of these
Answer: A
53) What is the total number of winning coalitions?
A) 1
B) 5
C) 3
D) 15 E) none of these
Answer: C
54) The Banzhaf power distribution of the weighted voting system is
A) P ₁ : 40%; P ₂ : 40%; P ₃ : 10%; P ₄ : 10%.
B) P ₁ : 25%; P ₂ : 25%; P ₃ : 25%; P ₄ : 25%.
C) P ₁ : 37.5%; P ₂ : 37.5%; P ₃ : 12.5%; P ₄ : 12.5%.
D) P ₁ : 40%; P ₂ : 30%; P ₃ : 20%; P ₄ : 10%.

E) none of these

Refer	to the weighted voting system [12:5, 5, 2, 2] and the Banzhaf definition of power. (The four players are P_1 , P_2 , P_3 ,
and P	74.)
	55) What is the weight of the coalition {Po. Po. Pa. Pa}?

- 55) What is the weight of the coalition $\{P_2, P_3, P_4\}$? A) 6 B) 9 C) 12 D) 10 E) none of these Answer: B 56) Which players in the coalition {P₁, P₂, P₃, P₄} are critical? A) All four players B) P₁ and P₂ C) P₁ only D) None of the players E) none of these Answer: B 57) What is the total number of winning coalitions? A) 15
- - B) 3
 - C) 5
 - D) 1
 - E) none of these

Answer: B

- 58) The Banzhaf power distribution of the weighted voting system is
 - A) P₁: 25%; P₂: 25%; P₃: 25%; P₄: 25%.
 - B) P₁: 37.5%; P₂: 37.5%; P₃: 12.5%; P₄: 12.5%.
 - C) P₁: 40%; P₂: 40%; P₃: 10%; P₄: 10%.
 - D) P₁: 40%; P₂: 30%; P₃: 20%; P₄: 10%.
 - E) none of these

Answer: B

Refer to the weighted voting system [25:16, 8, 6, 3] and the Banzhaf definition of power. (The four players are P₁, P₂, P₃ and P4.)

- 59) The weight of the coalition $\{P_1, P_2, P_3, P_4\}$ is
 - A) 33.
 - B) 17.
 - C) 34.
 - D) 39.
 - E) none of these

60) Which players are critical in the coalition {P ₁ , P ₃ , P ₄ }?
A) All three players
B) P ₁ and P ₃ only
C) None of the players
D) P ₁ only
E) none of these
Answer: A
61) Which players are critical in the coalition $\{P_1, P_2, P_3, P_4\}$?
A) P ₁ and P ₂ only
B) P ₁ only
C) All of the players
D) None of the players
E) none of these
Answer: B
62) Which players have veto power?
A) None of the players
B) P ₁ only
C) All of the players
D) P ₁ and P ₂ only
E) none of these
Answer: B
63) The winning coalitions are
A) all coalitions with three or more players, one of which is P ₁ .
B) all coalitions with two or more players.
C) all coalitions with three or more players.D) all coalitions with P₁ in it.
E) none of these
Answer: A
64) The number of winning coalitions is
A) 15.
B) 3. C) 4.
D) 5.
E) none of these
Answer: C
65) The Banzhaf power distribution of the weighted voting system is
A) P ₁ : 40%; P ₂ : 20%; P ₃ : 20%; P ₄ : 20%.
B) P ₁ : 25%; P ₂ : 25%; P ₃ : 25%; P ₄ : 25%.
C) P ₁ : 60%; P ₂ : 20%; P ₃ : 10%; P ₄ : 10%.
D) P ₁ : 50%; P ₂ : 30%; P ₃ : 10%; P ₄ : 10%.
E) none of these

Refer to the weighted voting system [25:16, 9, 9, 7] and the Banzhaf definition of power. (The four players are P_1 , P_2 , P_3 and P_4 .)

66) The weight of the coalition {P₁, P₃, P₄} is A) 32. B) 43. C) 41. D) 25. E) none of these Answer: A 67) Which players are critical in the coalition {P₁, P₃, P₄}? A) P₁ and P₃ only B) None of the players C) P₁ only D) All three players E) none of these Answer: A 68) Which players are critical in the coalition {P₁, P₂, P₃, P₄}? A) P₁, P₂, and P₃ only B) P₁ only C) All of the players D) P₁ and P₂ only E) None of the players Answer: E 69) In this weighted voting system, which players have veto power? A) P₁, P₂, and P₃ only B) All of the players C) P₁ only D) P₁ and P₂ only E) None of the players Answer: E 70) The winning coalitions are: A) {P₁, P₂}, {P₁, P₃}, and all coalitions with three or more players. B) all coalitions with two or more players. C) all coalitions with three or more players. D) all coalitions with P₁ in it. E) none of these Answer: A

71) The number of winning coalitions is

- A) 8.
- B) 5.
- C) 7.
- D) 15.
- E) none of these

Answer: C

72) The Banzhaf power distribution of the weighted voting system is

A)
$$P_1: \frac{1}{2}; P_2: \frac{1}{5}; P_3: \frac{1}{5}; P_4: \frac{1}{10}.$$

B)
$$P_1: \frac{7}{12}$$
; $P_2: \frac{1}{6}$; $P_3: \frac{1}{6}$; $P_4: \frac{1}{12}$.

C)
$$P_1: \frac{1}{3}; P_2: \frac{1}{4}; P_3: \frac{1}{4}; P_4: \frac{1}{6}.$$

D)
$$P_1: \frac{5}{12}$$
; $P_2: \frac{1}{4}$; $P_3: \frac{1}{4}$; $P_4: \frac{1}{12}$.

E) none of these

Answer: D

Refer to the weighted voting system [26:16, 9, 9, 7] and the Banzhaf definition of power. (The four players are P₁, P₂, P₃ and P4.)

73) Which players are critical in the coalition $\{P_1, P_3, P_4\}$?

- A) P₁ and P₃ only
- B) All three players
- C) P₁ only
- D) None of the players
- E) none of these

Answer: B

74) Which players are critical in the coalition $\{P_1, P_2, P_3, P_4\}$?

- A) P₁ and P₂ only
- B) P₁ only
- C) P₁, P₂ and P₃ only
- D) All of the players
- E) None of the players

Answer: B

75) In this weighted voting system, which players have veto power?

- A) All of the players
- B) P₁, P₂ and P₃ only
- C) P₁ only
- D) P₁ and P₂ only
- E) None of the players

- 76) The winning coalitions are
 - A) all coalitions with three or more players.
 - B) all coalitions with three or more players except for {P₂, P₃, P₄}.
 - C) only the grand coalition.
 - D) all coalitions with two or more players except for {P₃, P₄}.
 - E) none of these

Answer: B

- 77) The number of losing coalitions is
 - A) 11.
 - B) 4.
 - C) 14.
 - D) 1.
 - E) none of these

Answer: A

78) The Banzhaf power distribution of the weighted voting system is

A)
$$P_1: \frac{2}{5}; P_2: \frac{1}{5}; P_3: \frac{1}{5}; P_4: \frac{1}{5}$$
.

B)
$$P_1: \frac{1}{2}; P_2: \frac{1}{6}; P_3: \frac{1}{6}; P_4: \frac{1}{6}.$$

C)
$$P_1: \frac{1}{2}; P_2: \frac{3}{10}; P_3: \frac{1}{10}; P_4: \frac{1}{10}$$
.

D)
$$P_1: \frac{5}{12}; P_2: \frac{1}{4}; P_3: \frac{1}{4}; P_4: \frac{1}{12}.$$

E) none of these

Answer: A

Solve the problem.

- 79) The Banzhaf power index of player P₄ in the weighted voting system [10:3, 3, 3, 2] is
 - A) $\frac{1}{12}$
 - B) 0
 - C) $\frac{1}{4}$
 - D) $\frac{1}{6}$
 - E) none of these

Answer: C

Refer to the weighted voting system [22:10,8,6,4,2] and the Banzhaf definition of power. (The five players will be called P_1 , P_2 , P_3 , P_4 , and P_5 .)

- 80) The number of coalitions is
 - A) 63.
 - B) 15.
 - C) 31.
 - D) 120.
 - E) none of these

81) The number of coalitions having exactly two players is
A) 1
B) 20
C) 10
D) 5
E) none of these
Answer: C
82) The number of winning coalitions having exactly two players is
A) 5
B) 10
C) 1
D) 0
E) none of these
Answer: D
83) The number of coalitions having exactly three players is
A) 20
B) 10
C) 1
D) 5
E) none of these
Answer: B
84) The number of winning coalitions having exactly three players is
A) 5
B) 2
C) 10
D) 1
E) none of these
Answer: B
85) The number of coalitions having exactly four players is
A) 10
B) 20
C) 5
D) 1
E) none of these
Answer: C
86) The number of winning coalitions having exactly four players is
A) 2
B) 1
Ć) 3
D) 4
E) none of these
Answer: D

87) In this weighted voting system, A) P₃ has three times as much power as P₄. B) P₃ has twice as much power as P₄. C) P₃ has four times as much power as P₅. D) P₃ and P₄ have the same power. E) none of these Answer: D 88) In this weighted voting system, giving any individual player one more vote has the effect of A) giving that player no more power. B) giving that player 1/31 more power. C) giving that player 1/19 more power. D) giving that player 1/5 more power. E) none of these Answer: A Refer to the weighted voting system [24:10, 8, 6, 4, 2] and the Banzhaf definition of power. (The five players will be called P₁, P₂, P₃, P₄, and P₅.) 89) The number of coalitions is A) 31. B) 15. C) 63. D) 120. E) none of these Answer: A 90) The number of winning coalitions is A) 3. B) 10. C) 5. D) 15. E) none of these Answer: C 91) In this voting system,

A) P₃ and P₄ have the same power.
B) P₃ has twice as much power as P₄.
C) P₃ has four times as much power as P₅.
D) P₃ has three times as much power as P₄.

E) none of these

Answer: D

A committee consists of six members (A, B, C, D, E, and F). A has veto power; B, C, D, and E each have one vote. F is a nonvoting member. For a motion to pass it must have the support of A plus at least two additional voting members.

- 92) Which of the following is not a winning coalition?
 - A) {B, C, D, E}
 - B) {A, B, C, D}
 - C) {A, B, E}
 - D) {A, C, D, E}
 - E) none of these

Answer: A

- 93) Which are the critical players in the coalition {A, B, D}?
 - A) B only
 - B) A, B, and D
 - C) D only
 - D) A only
 - E) none of these

Answer: B

- 94) The Banzhaf power index of player A is
 - A) $\frac{7}{11}$
 - B) $\frac{1}{3}$
 - C) $\frac{5}{11}$
 - D) $\frac{11}{23}$
 - E) none of these

Answer: D

A committee consists of five members (A, B, C, D, and E). A and B have veto power; C, D, and E each have one vote. For a motion to pass it must have the support of both A and B plus at least one additional member.

- 95) Which of the following is not a winning coalition?
 - A) {B, C, D, E}
 - B) {A, B, C, D}
 - C) {A, B, C, D, E}
 - D) {A, B, E}
 - E) none of these

Answer: A

- 96) Which are the critical players in the coalition {A, B, D, E}?
 - A) E only
 - B) D only
 - C) A and B only
 - D) A, B, D and E
 - E) none of these

97) The Banzhaf power distribution of the committee is

A) A:
$$\frac{1}{5}$$
; B: $\frac{1}{5}$; C: $\frac{1}{5}$; D: $\frac{1}{5}$; E: $\frac{1}{5}$.

B) A:
$$\frac{7}{17}$$
; B: $\frac{7}{17}$; C: $\frac{1}{17}$; D: $\frac{1}{17}$; E: $\frac{1}{17}$.

C) A:
$$\frac{7}{20}$$
; B: $\frac{7}{20}$; C: $\frac{1}{10}$; D: $\frac{1}{10}$; E: $\frac{1}{10}$.

D) A:
$$\frac{7}{20}$$
; B: $\frac{7}{20}$; C: $\frac{3}{20}$; D: $\frac{1}{10}$; E: $\frac{1}{20}$.

E) none of these

Answer: B

Solve the problem.

98) Consider the generic weighted voting system $[q: w_1, w_2, w_3, w_4, w_5]$. Suppose that the winning coalitions are exactly those having 3 or more players. Compute the Banzhaf power index of player P_1 .

A)
$$\frac{1}{5}$$

B)
$$\frac{1}{10}$$

D)
$$\frac{1}{2}$$

E) none of these

Answer: A

99) Consider the generic weighted voting system $\{q: w_1, w_2, w_3, w_4, w_5\}$. Suppose that the winning coalitions are $\{P_1, P_2, P_3\}$, $\{P_1, P_2, P_3, P_4\}$, $\{P_1, P_2, P_3, P_5\}$, and $\{P_1, P_2, P_3, P_4, P_5\}$. Find the Banzhaf power distribution.

A)
$$P_1: \frac{1}{5}, P_2: \frac{1}{5}, P_3: \frac{1}{5}, P_4: \frac{1}{5}, P_5: \frac{1}{5}$$

B)
$$P_1: \frac{5}{16}$$
, $P_2: \frac{5}{16}$, $P_3: \frac{1}{4}$, $P_4: \frac{1}{16}$, $P_5: \frac{1}{16}$

C)
$$P_1: \frac{1}{4}$$
, $P_2: \frac{1}{4}$, $P_3: \frac{1}{4}$, $P_4: \frac{1}{8}$, $P_5: \frac{1}{8}$

D)
$$P_1: \frac{1}{3}, P_2: \frac{1}{3}, P_3: \frac{1}{3}, P_4: 0, P_5: 0$$

E) none of these

Answer: D

100) In the weighted voting system [21:12, 8, 6, 3, 2], the total number of possible coalitions is

- A) 23.
- B) 32.
- C) 31.
- D) 63.
- E) none of these

101) In the weighted voting system [21:10, 8, 5, 3, 2], the total number of possible coalitions is

- A) 31.
- B) 16.
- C) 63.
- D) 32.
- E) none of these

Answer: A

Refer to the weighted voting system [10:7,5,4] and the Shapley-Shubik definition of power. (The three players are P_1 , P_2 , and P_3 .)

102) Which player in the sequential coalition $\langle P_1, P_2, P_3 \rangle$ is pivotal?

- A) P₂
- B) P₁
- C) P3
- D) All three players
- E) none of these

Answer: A

103) Which player in the sequential coalition $\langle P_3, P_2, P_1 \rangle$ is pivotal?

- A) P₁
- B) P3
- C) P2
- D) All three players
- E) none of these

Answer: A

104) In how many sequential coalitions is P2 the pivotal player?

- A) 6
- B) 0
- C) 2
- D) 1
- E) none of these

Answer: D

105) The Shapley-Shubik power distribution of the weighted voting system is

- A) $P_1: \frac{1}{2}; P_2: \frac{1}{2}; P_3: 0.$
- B) $P_1: \frac{2}{3}; P_2: \frac{1}{6}; P_3: \frac{1}{6}$.
- C) $P_1: \frac{1}{3}; P_2: \frac{1}{3}; P_3: \frac{1}{3}$.
- D) $P_1: \frac{1}{2}; P_2: \frac{1}{3}; P_3: \frac{1}{6}$.
- E) none of these

Refer to the weighted voting system [8: 6, 3, 2] and the Shapley-Shubik definition of power. (The three players are P_1 , P_2 , and P_3 .)

- 106) Which player in the sequential coalition $\langle P_1, P_2, P_3 \rangle$ is pivotal?
 - A) P3
 - B) P2
 - C) P₁
 - D) All three players
 - E) none of these

Answer: B

- 107) Which player in the sequential coalition $\langle P_3, P_2, P_1 \rangle$ is pivotal?
 - A) P₂
 - B) P3
 - C) P₁
 - D) All three players
 - E) none of these

Answer: C

- 108) In how many sequential coalitions is P₂ the pivotal player?
 - A) 0
 - B) 1
 - C) 6
 - D) 2
 - E) none of these

Answer: B

- 109) The Shapley-Shubik power distribution of the weighted voting system is
 - A) $P_1: \frac{1}{2}; P_2: \frac{1}{3}; P_3: \frac{1}{6}$.
 - B) $P_1: \frac{2}{3}; P_2: \frac{1}{6}; P_3: \frac{1}{6}$.
 - C) $P_1: \frac{1}{3}; P_2: \frac{1}{3}; P_3: \frac{1}{3}$.
 - D) $P_1: \frac{1}{2}; P_2: \frac{1}{2}; P_3: 0.$
 - E) none of these

Refer to the weighted voting system [10:7,6,4] and the Shapley-Shubik definition of power. (The three players are P_1 , P_2 , and P_3 .)

- 110) Which player in the sequential coalition $\langle P_3, P_2, P_1 \rangle$ is pivotal?
 - A) P₂
 - B) P₁
 - C) P3
 - D) All three players
 - E) none of these

Answer: A

- 111) In how many sequential coalitions is P₂ the pivotal player?
 - A) 1
 - B) 0
 - C) 2
 - D) 6
 - E) none of these

Answer: C

- 112) The Shapley-Shubik power distribution of the weighted voting system is
 - A) $P_1: \frac{1}{2}; P_2: \frac{1}{3}; P_3: \frac{1}{6}$.
 - B) P₁: $\frac{1}{2}$; P₂: $\frac{1}{2}$; P₃: 0.
 - C) $P_1: \frac{2}{3}; P_2: \frac{1}{6}; P_3: \frac{1}{6}$.
 - D) $P_1: \frac{1}{3}; P_2: \frac{1}{3}; P_3: \frac{1}{3}$.
 - E) none of these

Answer: D

Refer to the weighted voting system [9:4,3,2,1] and the Shapley-Shubik definition of power. (The four players will be called P_1 , P_2 , P_3 , and P_4 .)

- 113) The number of sequential coalitions is
 - A) 31.
 - B) 24.
 - C) 16.
 - D) 6.
 - E) none of these

114) The Shapley-Shubik power index of player P ₄ is
A) $\frac{1}{10}$.
B) $\frac{1}{9}$.
C) 0.
D) $\frac{1}{4}$.
E) none of these
Answer: C
115) The number of sequential coalitions is
A) 6.
B) 16.
C) 32.
D) 24.
E) none of these
Answer: D
116) Which player in the sequential coalition $\langle P_1, P_2, P_3, P_4 \rangle$ is pivotal?
A) P ₂
B) P ₃
C) P ₁
D) P ₄
E) none of these
Answer: B
117) Which player in the sequential coalition $\langle P_2, P_3, P_4, P_1 \rangle$ is pivotal?
A) P_1
B) P ₂
C) P ₃
D) P ₄
E) none of these
Answer: A
118) In how many sequential coalitions is player P ₄ pivotal?
A) 6
B) 1
C) 0
D) 2
E) none of these
Answer: C

119) The Shapley-Shubik power distribution of the weighted voting system is

A)
$$P_1: \frac{1}{4}; P_2: \frac{1}{4}; P_3: \frac{1}{4}; P_4: \frac{1}{4}.$$

B)
$$P_1: \frac{5}{12}; P_2: \frac{1}{3}; P_3: \frac{5}{24}: P_4: \frac{1}{24}.$$

C)
$$P_1: \frac{1}{3}; P_2: \frac{1}{3}; P_3: \frac{1}{3}; P_4: 0.$$

D)
$$P_1: \frac{2}{3}; P_2: \frac{1}{6}; P_3: \frac{1}{6}; P_4: 0.$$

E) none of these

Answer: C

Refer to the weighted voting system [22:10, 8, 6, 4, 2] and the Shapley-Shubik definition of power. (The five players will be called P_1 , P_2 , P_3 , P_4 , and P_5 .)

120) In how many sequential coalitions is player P5 pivotal?

- A) 12
- B) 6
- C) 36
- D) 24
- E) none of these

Answer: B

121) If player P5 is pivotal in a sequential coalition, which player does not appear before P5?

- A) P₅ is never pivotal
- B) P₂
- C) P3
- D) P₄
- E) P₁

Answer: B

122) In how many sequential coalitions is player P₄ pivotal?

- A) 16
- B) 10
- C) 24
- D) 4
- E) none of these

- A) $\frac{1}{10}$.
- B) $\frac{1}{20}$
- C) $\frac{3}{10}$.
- D) $\frac{1}{5}$.

E) none of these

Answer: B

Refer to the weighted voting system [26:10,8,6,4,2] and the Shapley-Shubik definition of power. (The five players will be called P_1 , P_2 , P_3 , P_4 , and P_5 .)

124) In how many sequential coalitions is player P5 pivotal?

- A) 36
- B) 12
- C) 24
- D) 6
- E) none of these

Answer: D

125) In how many sequential coalitions is player P₁ pivotal?

- A) 24
- B) 36
- C) 6
- D) 12
- E) none of these

Answer: B

126) The Shapley-Shubik power index of player P₅ is

- A) $\frac{1}{5}$.
- B) $\frac{3}{10}$.
- C) $\frac{1}{20}$.
- D) $\frac{1}{10}$.
- E) none of these

Sol

lve the problem.	
	power index of player P ₄ in the weighted voting system [10: 3, 3, 3, 2] is
A) 0	
B) $\frac{1}{12}$	
C) $\frac{1}{4}$	
D) $\frac{1}{6}$	
E) none of these	
Answer: C	
with three players? A) 0	ng is not a possible Shapley-Shubik power index for a player in a weighted voting system
B) $\frac{1}{3}$	
C) $\frac{1}{4}$	
D) $\frac{1}{2}$	
E) none of these	
Answer: C	
129) Which of the following with four players? A) $\frac{1}{4}$	ng is not a possible Shapley-Shubik power index for a player in a weighted voting system
4	
B) $\frac{1}{6}$	
C) $\frac{1}{3}$	
D) $\frac{1}{5}$	
E) none of these	
Answer: D	
12 times and P ₂ is pi	weighted voting system [q: w_1 , w_2 , w_3 , w_4]. Suppose that $w_2 = w_3$, P_1 is a pivotal player votal 4 times. What is the Shapley–Shubik power index of P_4 ?
A) $\frac{1}{2}$	
B) $\frac{1}{6}$	
C) $\frac{1}{3}$	
D) 0	

E) Can't be determined from the given information.

- 131) In the weighted voting system [17:10, 7, 5, 3, 1], the total number of possible sequential coalitions involving all five players is
 - A) 31.
 - B) 720.
 - C) 24.
 - D) 120.
 - E) none of these

Answer: D

- 132) In the weighted voting system [21:10, 8, 5, 3, 2], the total number of possible sequential coalitions involving all five players is
 - A) 720.
 - B) 16.
 - C) 120.
 - D) 24.
 - E) none of these

Answer: C

- 133) $\frac{100!}{98!}$ =
 - A) 9,900
 - B) 199
 - C) 100
 - D) 2
 - E) none of these

Answer: A

- 134) $\frac{200!}{198!}$ =
 - A) 399
 - B) 200
 - C) 2
 - D) 39,800
 - E) none of these

Answer: D

- 135) 99! + 100! =
 - A) $2 \times 100! 100$
 - B) 199!
 - C) 101 x 99!
 - D) 2 × 99! + 100
 - E) none of these

Answer: C

- 136) 199! + 200! =
 - A) $2 \times 199! + 200$
 - B) $2 \times 200! 200$
 - C) $201 \times 199!$
 - D) 399!
 - E) none of these

137) 300! – 299! =	
A) $299^2 \times 298!$	
B) 1	
C) 300 – 2 × 299!	
D) 299 x 299!	
E) none of these	
Answer: D	
138) A, B, C, D, E and F are the starting six players on a hockey team. The coach must choose a set of honorary	Ÿ
"captains" for the last game of the season – it can be any number from one to all six. How many different	
possibilities are there?	
A) 720	
B) 63	
C) 35	
D) 6	
E) none of these	
Answer: B	
139) A, B, C, D, and E are the starting five players in a basketball team. The coach must choose a set of honora	ıry
"captains" for the last game of the season – it can be any number from one to all five. How many differer	ıt
possibilities are there?	
A) 31	
B) 24	
C) 120	
D) 5	
E) none of these	
Answer: A	
140) The Tasmania State University football team has 11 starting players on their offense. The coach must sele	
order in which they will be introduced for the last game of the season. How many different possibilities	are
there?	
A) 11!	
B) 11 ²	
C) 2 ¹¹ - 1	
D) 11	
E) none of these	
Answer: A	
141) A weighted voting system has 100 players. How many coalitions of size 99 are possible?	
A) 100	
B) 50	
C) 99	
D) 1	
E) none of these	

142) A weighted voting system has 100 players. How many coalitions of size 98 are possible? A) 98 B) 4900 C) 8900 D) 4950 E) none of these Answer: D
143) A weighted voting system has 100 players. How many sequential coalitions in which P ₅₀ is listed first are
possible? A) 50! B) 100! – 1 C) $\frac{100!}{50}$ D) 99! E) none of these Answer: D
 144) Consider the generic weighted voting system [q: w₁, w₂, w₃, w₄, w₅]. Suppose that the winning coalitions are exactly those having 3 or more players. Which players are critical in the coalition {P₁, P₂, P₄, P₅}? A) P₁, P₂, P₄, P₅ B) P₁ only C) P₁, P₂, and P₄ D) None of the players E) none of these Answer: D
145) Consider the generic weighted voting system (g. wa. we. we. w. w.) Suppose that the winning coalitions are
 145) Consider the generic weighted voting system {q: w₁, w₂, w₃, w₄, w₅}. Suppose that the winning coalitions are {P₁, P₂, P₃}, {P₁, P₂, P₃, P₄}, {P₁, P₂, P₃, P₅}, and {P₁, P₂, P₃, P₄, P₅}. Which players are critical in the grand coalition {P₁, P₂, P₃, P₄, P₅}? A) P₁, P₂, and P₃ B) P₁, P₂, P₃, and P₄ C) P₁ only D) None of the players E) none of these Answer: A
146) Consider the generic weighted voting system {q: w ₁ , w ₂ , w ₃ , w ₄ , w ₅ }. Suppose that the winning coalitions are {

 $P_1, P_2, P_3\}, \{P_1, P_2, P_3, P_4\}, \{P_1, P_2, P_3, P_5\}, and \{P_1, P_2, P_3, P_4, P_5\}. Which players have veto power?$

- A) P₁, P₂, and P₃
- B) P₁ only
- C) P₁, P₂, P₃, and P₄
- D) None of the players
- E) All of the players

147) In any weighted voting system having N players, what is the minimum number of winning coalitions possible? A) 0 B) N C) 1 D) N - 1 E) none of these Answer: C
148) In any weighted voting system having N players, what is the maximum number of players that can have veto power? A) N B) N - 1 C) 2 D) 1 E) none of these Answer: A
 149) Two weighted voting systems are equivalent if they have the same number of players and exactly the same winning coalitions. Which of the following weighted voting systems are equivalent to [5:3, 2, 1, 1]? A) [9:5, 4, 3, 1] B) [8:4, 3, 2, 1] C) [6:3, 2, 1, 1] D) [10:6, 5, 4, 2] E) [7:3, 2, 1, 1] Answer: A